

2_G7. Operations with Rational Numbers

Materials: screening cards
two-color chips, number line

available:

Place a screening card in front of student one at a time, and ask, “What is the answer to this problem?” If needed, follow up: “How did you figure out your answer?” Have optional manipulatives available.

- A. $-3 + 7$
- B. $-5 - 1\frac{2}{3}$
- C. $-\frac{1}{2} - -1\frac{3}{4}$

Abilities	Challenges/Strategies	Notes
<p>Identifies</p> <ul style="list-style-type: none"> <input type="checkbox"/> 4 <input type="checkbox"/> $-6\frac{2}{3}$ <input type="checkbox"/> $1\frac{1}{4}$ <input type="checkbox"/> Understands interaction of negative and positive values <input type="checkbox"/> Correctly works with fractions and/or mixed numbers <input type="checkbox"/> Explains approach / justifies thinking 	<p>Unable to identify:</p> <ul style="list-style-type: none"> <input type="checkbox"/> 4 <input type="checkbox"/> $-6\frac{2}{3}$ <input type="checkbox"/> $1\frac{1}{4}$ <input type="checkbox"/> Computes with positive values, but doesn't take into account negative value <input type="checkbox"/> Challenged with fraction operations 	

Fraction Addition & Subtraction Strategies (6_G5)

Materials: screening cards

available: fraction circle/ bars, # lines, grid paper

Place a card in front of the student and ask, “What is the answer to this problem?” If needed, follow up: “How did you figure out your answer?”

- A. $\frac{5}{8} + \frac{3}{12}$
- B. $1\frac{4}{5} + 4\frac{1}{4}$
- C. $4\frac{1}{2} - 2\frac{1}{3}$

Abilities	Challenges/Strategies	Notes
<p>Identifies:</p> <ul style="list-style-type: none"> <input type="checkbox"/> $\frac{5}{8} + \frac{3}{12} = \frac{21}{24}$ or $\frac{7}{8}$ <input type="checkbox"/> $1\frac{4}{5} + 4\frac{1}{4} = 5\frac{21}{20}$ or $6\frac{1}{20}$ <input type="checkbox"/> $4\frac{1}{2} - 2\frac{1}{3} = 2\frac{1}{6}$ <input type="checkbox"/> Understands need for common denominator <input type="checkbox"/> Explains approach 	<p>Unable to identify:</p> <ul style="list-style-type: none"> <input type="checkbox"/> $\frac{4}{16}$ (four-sixteenths or equiv) <input type="checkbox"/> $-\frac{4}{5}$ (negative four-fifths) 	

3_G7. Rational Numbers Multiplication/Division

Materials: screening cards
available: paper and pencil

Show each card and ask students to use what they know about fraction operations to determine whether the product/quotient is less than or greater than the benchmark, rather than work out an exact answer. If needed, follow up: “How do you know?”

A. $\frac{4}{7} \times -\frac{1}{2}$

“Using what you know about fraction operations, is the product less than $-\frac{1}{2}$ or greater than $-\frac{1}{2}$?”

B. $-\frac{2}{3} \div -\frac{1}{2}$

“Using what you know about fraction operations, is the quotient less than $-\frac{2}{3}$ or greater than $-\frac{2}{3}$?”

Abilities	Challenges/Strategies	Notes
<input type="checkbox"/> $\frac{4}{7} \times -\frac{1}{2} > -\frac{1}{2}$ <input type="checkbox"/> Sound justification <input type="checkbox"/> $-\frac{2}{3} \div -\frac{1}{2} > -\frac{2}{3}$ <input type="checkbox"/> Sound justification	<input type="checkbox"/> $\frac{4}{7} \times -\frac{1}{2} < -\frac{1}{2}$ <input type="checkbox"/> $-\frac{2}{3} \div -\frac{1}{2} < -\frac{2}{3}$ <input type="checkbox"/> Unable to justify <input type="checkbox"/> Challenged by negative values <input type="checkbox"/> Challenged by fractional values <input type="checkbox"/> Misconception: multiplication makes it larger, which is why it's greater <input type="checkbox"/> Misconception: Division makes it smaller <input type="checkbox"/> Only computes, rather than reasons	

Estimating Fraction Quotients (6_G6)

Materials: screening cards
available: paper and pencil

Show each card and ask students to use what they know about fraction operations to determine whether the quotient is less than or greater than the benchmark, rather than work out an exact answer. If needed, follow up: “How do you know?”

A. $\frac{5}{11} \div \frac{3}{4}$

“Using what you know about fraction operations, is the quotient less than 1 or greater than 1?”

B. $2\frac{1}{8} \div \frac{1}{4}$

“Using what you know about fraction operations, is the quotient less than 4 or greater than 4?”

Abilities	Challenges/Strategies	Notes
<input type="checkbox"/> $\frac{5}{11} \div \frac{3}{4} < 1$ <input type="checkbox"/> Sound justification <input type="checkbox"/> $2\frac{1}{8} \div \frac{1}{4} > 4$ <input type="checkbox"/> Sound justification	<input type="checkbox"/> $\frac{5}{11} \div \frac{3}{4} > 1$ <input type="checkbox"/> $2\frac{1}{8} \div \frac{1}{4} < 4$ <input type="checkbox"/> Unable to justify	

Estimating Fraction Products & Quotients (7_G5)

Materials: screening cards, available paper and pencil

Show each card and ask students to use what they know about fraction operations to determine whether the quotient is less than or greater than the benchmark, rather than work out an exact answer. If needed, follow up: “How do you know?”

A. $2 \times \frac{4}{5}$

“Using what you know about fraction operations, is the product less than $\frac{4}{5}$ or greater than $\frac{4}{5}$?”

B. $\frac{2}{3} \times \frac{9}{10}$

“Using what you know about fraction operations, is the product less than $\frac{9}{10}$ or greater than $\frac{9}{10}$?”

C. $3 \div \frac{1}{8}$

“Using what you know about fraction operations, is the quotient less than 3 or greater than 3?”

Abilities	Challenges/Strategies	Notes
<ul style="list-style-type: none"> <input type="checkbox"/> Greater than $\frac{4}{5}$ <input type="checkbox"/> Less than $\frac{9}{10}$ <input type="checkbox"/> Greater than 3 <input type="checkbox"/> Reasons about fractions and multiplication (2 times is doubling; $\frac{2}{3}$ of a number less is less than that number) <input type="checkbox"/> Reasons about fraction division (3 has how many $\frac{1}{8}$) 	<ul style="list-style-type: none"> <input type="checkbox"/> Misconception: multiplication always makes bigger <input type="checkbox"/> Misconception: division always makes smaller <input type="checkbox"/> Computes rather than estimates <input type="checkbox"/> Other 	

4_G7. Percent Problems**Materials:** screening cards available: paper and pencil

Place a screening card in front of the student one at a time, and ask, "What is the answer to this problem?" If needed, follow up: "How did you figure out your answer?"

- A. What is the total cost? Item \$20, Tax Rate 5%
 B. What is the sale price? Item \$40, Sale 20% off

Abilities	Challenges/Strategies	Notes
<input type="checkbox"/> Total cost: \$21 <input type="checkbox"/> Sound justification <input type="checkbox"/> Sale price: \$32 <input type="checkbox"/> Sound justification	<input type="checkbox"/> Total cost: _____ <input type="checkbox"/> Sale price: _____ <input type="checkbox"/> Unable to justify <input type="checkbox"/> Calculates percentage, but not final price <input type="checkbox"/> Circle Strategy: Benchmark percentages; Proportion/equation; Other	

Percent of a Quantity (3_G6)**Materials:** screening cards; available: paper and pencil

A. Place a screening card in front of student one at a time, and ask, "What is the answer to this problem?" If needed, follow up: "How did you figure out your answer?"

- B. What is 5% of 30? B. 6 is what % of 24? C. 30% of what is 6?

Abilities	Challenges/Strategies	Notes
<input type="checkbox"/> 5% of 30 is <u>1.5</u> <input type="checkbox"/> Sound justification <input type="checkbox"/> 6 is <u>25%</u> is 24 <input type="checkbox"/> Sound justification <input type="checkbox"/> 30% of <u>20</u> is 6 <input type="checkbox"/> Sound justification	<input type="checkbox"/> 5% of 30 is ____ <input type="checkbox"/> 6 is ____% is 24 <input type="checkbox"/> 30% of ____ is 6 <input type="checkbox"/> Unable to justify	

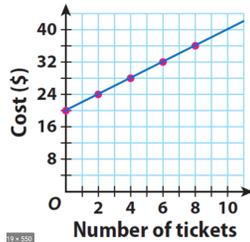
5_G7. Proportional Relationships

Materials: screening cards;
available: paper and pencil

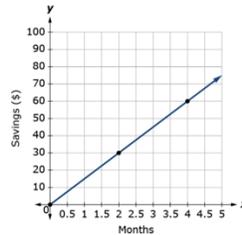
Spread the 6 cards in the set out in front of the student and ask, “Which of these relationships show a proportional relationship between 2 quantities?”

A. $3x = y$

B.



C.

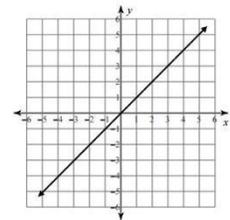


D.

x	y
0	0
4	8
7	14

E. $y = 2x + 5$

F.



Abilities

- Proportional Relationships: A, C, D, F
- Sound justification

Challenges/Strategies

- Unable to explain proportional relationships for:
 - equation
 - graph
 - table

Notes

Equivalent Ratios (4_G6)

Materials: screening cards;
available: paper and pencil

Place a screening card in front of the student one at a time, and ask, “What missing amount will make the ratios equivalent?” If needed, follow up: “How did you figure out your answer?”

A. $4 : 7 = _ : 21$

B. $12 : _ = 4 : 3$

Abilities

- $4 : 7 = 12 : 21$
- Sound justification
- $12 : 9 = 4 : 3$
- Sound justification

Challenges/Strategies

- $4 : 7 = _ : 21$
- $12 : _ = 4 : 3$
- Unable to justify

Notes

6_G7. Unit Rates		Materials: screening cards
<p>Place the problem cards in front of the student one at a time, and say, “What is the answer to this problem?” Once, the student responds, ask, “How do you know?”</p> <p>A. Ana earns \$50 in 4 hours. How much does she earn per hour? B. Jayden earns \$36 in 3 hours. Does Ana or Jayden earn more per hour? C. \$56 for 8 pounds of almonds, \$77 for 10 pounds of walnuts. Which costs less per pound?</p>		
Abilities	Challenges/Strategies	Notes
<input type="checkbox"/> \$12.50 per hour <input type="checkbox"/> Sound justification <input type="checkbox"/> Sound justification that Ana earns more per hour, with Jayden earning \$12/hour. <input type="checkbox"/> Almonds: \$7/lb; Walnuts: \$7.70/lb. <input type="checkbox"/> Sound justification that almonds cost less per pound.	<input type="checkbox"/> Unable to find unit rates <input type="checkbox"/> Reasons based on total earned or costs, rather than unit rates. <input type="checkbox"/> Unable to justify <input type="checkbox"/> Incorrect choices: _____	
Ratio Word problems (5_G6)		Materials: screening cards
<p>Place the problem cards in front of the student one at a time, and say, “Which is a better deal.” Once, the student chooses, ask, “How do you know?”</p> <p>A. \$23 for 2 pounds fish, \$11 for a pound of fish B. \$7 for 9 pounds of flour, \$8 for 10 pounds of flour</p>		
Abilities	Challenges/Strategies	Notes
<input type="checkbox"/> Chooses \$11 for a lb. <input type="checkbox"/> Sound justification <input type="checkbox"/> Chooses \$7 for 9 <input type="checkbox"/> Sound justification	<input type="checkbox"/> Incorrect choice _____ <input type="checkbox"/> Incorrect choice _____ <input type="checkbox"/> Unable to justify	

7_G7. Algebraic Expressions**Materials:** screening cards

Place the pair of expression cards in front of the student one at a time, and say, "Are these expressions equivalent?" Follow up with, "How do you know?"

- A. $3x + 5 + 7x$ $10x + 5$
 B. $4(x - 8)$ $4x - 8$
 C. $-5(x - 8) + 2$ $-5x - 38$

Abilities	Challenges/Strategies	Notes
<input type="checkbox"/> $3x + 5 + 7x$ equivalent to $10x + 5$ <input type="checkbox"/> Sound justification <input type="checkbox"/> $4(x - 8)$ not equivalent to $4x - 8$ <input type="checkbox"/> Sound justification <input type="checkbox"/> $-5(x - 8) + 2$ not equivalent to $-5x - 38$ <input type="checkbox"/> Sound justification	<input type="checkbox"/> Not Equivalent <input type="checkbox"/> Equivalent <input type="checkbox"/> Equivalent <input type="checkbox"/> Unable to justify	

Algebraic Expressions (8_G6)**Materials:** screening cards
Available: paper and pencil

Place the pair of expression cards in front of the student one at a time, and say, "Are these expressions equivalent?" Follow up with, "How do you know?"

- A. $3 + 4n + 1$ $8n$ B. $2(m + 3)$ $2m + 3$

Abilities	Challenges/Strategies	Notes
<input type="checkbox"/> $3 + 4n + 1$ Not Equivalent to $8n$ <input type="checkbox"/> Sound justification <input type="checkbox"/> $2(m+3)$ Not Equivalent to $2m+3$ <input type="checkbox"/> Sound justification	<input type="checkbox"/> Equivalent <input type="checkbox"/> Equivalent <input type="checkbox"/> Unable to justify	

8_G7. Word Problems

Materials: screening cards;
available: paper and pencil

Place the word problem card in front of the student and say, “Read the problem on this card.” Next spread the remaining cards in the set out in front of the student and ask,

- A. The length of a box is 3 more than twice its width. Let l represent the length of the box and w represent the width of the box. “Choose all of the equations that could represent the given situation.” Follow up: How do you know?

$$l - 3 = 2w \quad l + 3 = 2w \quad l = 2w + 3 \quad l - \frac{3}{2} = 2 \quad \frac{1}{2} - 3 = w \quad l = 2(w + 3)$$

- B. A puppy weighed 14 ounces at birth. It gains 2 ounces each week. Let x represent the number of weeks. How much does it weigh after x weeks? “Which of these cards is an equation that could represent the given situation?” Follow up: “How do you know?”

$$y = 14x + 2 \quad y = 2x + 14 \quad x = 2y + 14 \quad y - 14 = 2x \quad y - 14/2 = x \quad y/2 + 7 = x$$

Abilities	Challenges/Strategies	Notes
<p>Represents situation:</p> <p><input type="checkbox"/> $l - 3 = 2w$</p> <p><input type="checkbox"/> Sound justification</p> <p><input type="checkbox"/> $l = 2w + 3$</p> <p><input type="checkbox"/> Sound justification</p> <p>Does not represent situation:</p> <p>$l + 3 = 2w;$ $l - 3/2 = 2$</p> <p>$1/2 - 3 = w;$ $l = 2(w + 3)$</p> <p>Represents situation:</p> <p><input type="checkbox"/> $y = 2x + 14$</p> <p><input type="checkbox"/> Sound justification</p> <p><input type="checkbox"/> $y - 14 = 2x$</p> <p><input type="checkbox"/> Sound justification</p> <p>Does not represent situation:</p> <p>$y = 14x + 2;$ $x = 2y + 14$</p> <p>$y - 14/2 = x;$ $y/2 + 7 = x$</p>	<p><input type="checkbox"/> Incorrect choices:</p> <p><input type="checkbox"/> Unable to justify</p> <p><input type="checkbox"/> Incorrect Choices:</p> <p><input type="checkbox"/> Unable to justify</p>	

Word Problems (9_G6)

Materials: screening cards;
available: paper and pencil

Place the word problem card in front of the student and say, "Read the problem on this card."
Next, spread the remaining cards in the set out in front of the student and ask,
A school group is preparing for a field trip to a science center. There will be 7 times as many students as teachers on the trip.

- A. "Which card is an equation that represents the relationship in the problem?"
B. "Are there other cards that also represent this problem? If so which one/one? If not, why not?"

$$7s = t \quad t = \frac{1}{7} s \quad 7t = s \quad 7 = \frac{s}{t} \quad \frac{t}{s} = 7$$

Abilities	Challenges/Strategies	Notes
<p>Represents Relationship</p> <p><input type="checkbox"/> $t = \frac{1}{7} s$</p> <p><input type="checkbox"/> Sound justification</p> <p><input type="checkbox"/> $7t = s$</p> <p><input type="checkbox"/> Sound justification</p> <p><input type="checkbox"/> $7 = \frac{s}{t}$</p> <p><input type="checkbox"/> Sound justification</p> <p>Does Not Represent Relationship</p> <p><input type="checkbox"/> $7s = t$</p> <p><input type="checkbox"/> Sound justification</p> <p><input type="checkbox"/> $7 = \frac{t}{s}$</p> <p><input type="checkbox"/> Sound justification</p>	<p>Incorrect Choices:</p> <p><input type="checkbox"/> $7s = t$</p> <p><input type="checkbox"/> $7 = \frac{t}{s}$</p> <p><input type="checkbox"/> Unable to justify</p>	